

Introduction

The Center for Orbit Determination in Europe (CODE) is contributing to the IGS Multi-GNSS Extension (MGEX) since its start in 2012 with an orbit and clock solution. CODE's MGEX (COM) product includes the satellite systems GPS, GLONASS, Galileo, BeiDou2 (BDS2), and QZSS. GEO satellites are not included, so far.

The ECOM2 solar radiation pressure (SRP) model, used for all satellites in the COM solution, has been designed for yaw-steering (YS) attitude. Consequently, the orbit quality was degraded for BDS2 and QZS-1 spacecrafts (SC) at times when operating under orbit-normal (ON) attitude, i.e., during or close to eclipse seasons.

Here we introduce a family of empirical SRP models tailored for the ON-mode, which can either be used on top of an a priori SRP model or as a stand-alone model.

SRP in YS- and ON-modes

Features of the YS attitude mode are:

- solar panel (SP) plane is always parallel to the terminator plane and normal to the vector Sun => satellite (D)
- SC's Y-sides are never illuminated (Y=0, apart from Y-bias)
- SC body (+Z, -Z, +X panels) causes an SRP signal, which is periodic w.r.t. the argument of latitude difference betw. SC and Sun (Δu)
- rapid noon/midnight turns for small elevation angles (β) of the Sun w.r.t. the orbital plane

Features of the ON attitude mode are:

- no noon and midnight turns
- SP-normal (SPN) deviates from the vector D by the β -angle
- power generation is reduced compared to the YS-mode
- SRP due to SP can be absorbed by 2 SRP parameters, which are constant w.r.t. Δu , but not w.r.t. β
- all panels of SP body can be illuminated - causing periodic SRP signals w.r.t. Δu and β

Attitude Modes

Most GNSS SCs are oriented with YS attitude. Some BDS2 satellites and QZS-1 switch to ON attitude for small elevation angles β of the Sun w.r.t. the orbital plane. All GEO spacecrafts maintain the ON attitude permanently.

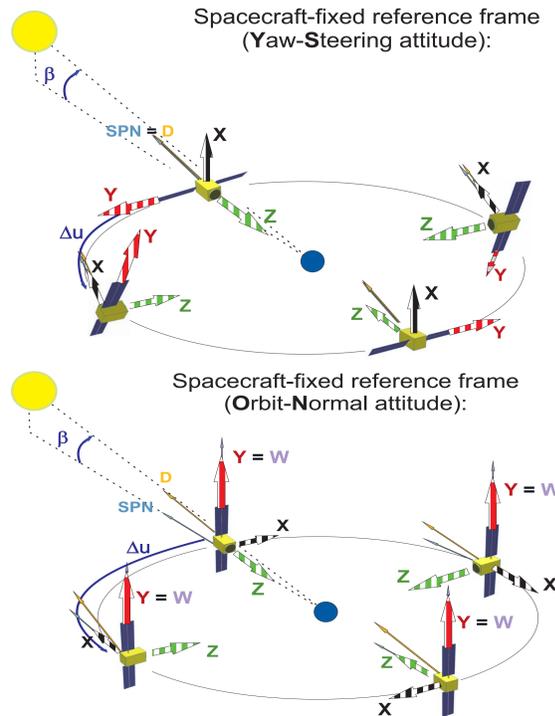


Fig. 1: Satellite-fixed ref. frames under YS- and ON-mode.

ECOM SRP Model Frames

During YS-mode the co-rotating ECOM decomposition is practical (SRP due to solar panels absorbed by one coeff.; Y=0). For ON-mode non-rotating frames are better suited (e.g., frames fixed to local orbit or orbital plane). We use the Terminator System Decomposition (TERM).

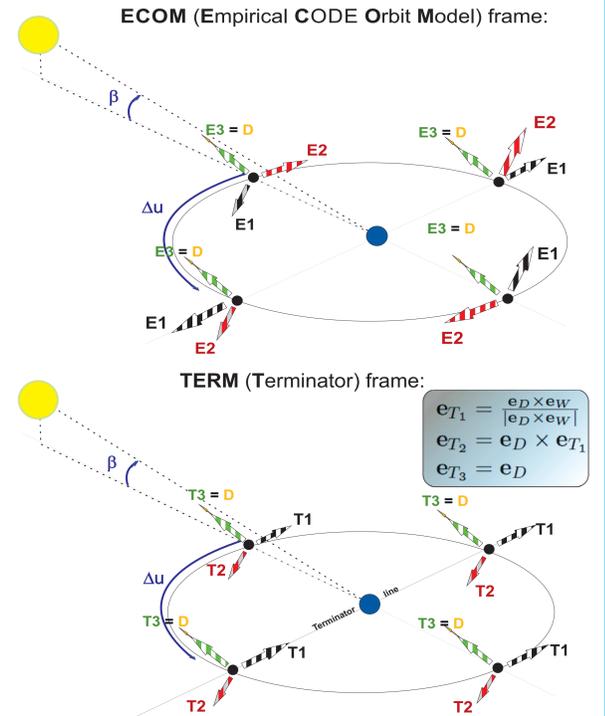


Fig. 2: SRP model frame definition.

SRP Simulation for ON

Simulations based on released meta data of QZS-1 have been performed separately for SP and SC body. Simulated SRP acceleration has been projected into the terminator reference frame (TERM, Fig. 2). Coefficients of significant size have been selected for ECOM-T (Δu) and ECOM-TB ($\Delta u, \beta$) - empirical SRP models for the ON-mode.

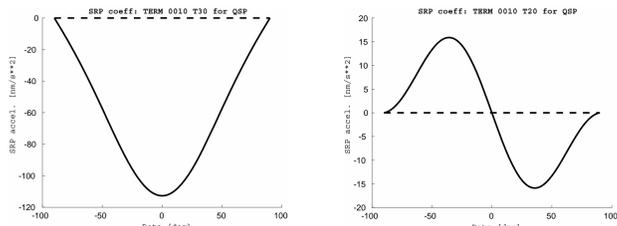


Fig. 3: Simulated SRP due to SP in TERM system.

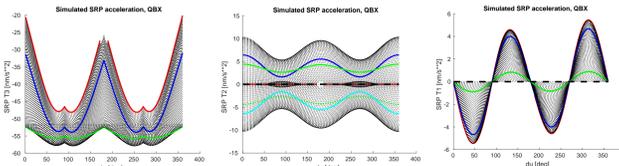


Fig. 4: Simulated SRP due to SC box in TERM system. Colors represent following β -angles: green, dotted: -80° , cyan: -30° , red: 0° , blue: $+30^\circ$, green, solid: $+80^\circ$.

Definition of ECOM-TBM

- version with just 2 SRP parameters covering SRP due to SP:

$$\begin{aligned} T3(\Delta u, \beta) &= T30C1b \cos \beta \\ T2(\Delta u, \beta) &= T20S2b \sin 2\beta \\ T1(\Delta u, \beta) &= 0 \end{aligned}$$

- β can be ignored for short-arcs => ECOM-TM (T20, T30)
- SRP due to sat.-body may be absorbed by stochastic orbit parameters (ECOM-TBMP) or by an a priori box model

Definition of ECOM-TB

- SRP acceleration during ON described in TERM system as ...

$$\mathbf{a} = \mathbf{a}_0 + T1(\Delta u, \beta) \mathbf{e}_{T1} + T2(\Delta u, \beta) \mathbf{e}_{T2} + T3(\Delta u, \beta) \mathbf{e}_{T3}$$

- ... by 9 SRP parameters:

$$\begin{aligned} T3(\Delta u, \beta) &= T30C1b \cos \beta + T3C2uC1b \cos 2\Delta u \cos \beta \\ &\quad + T3S2uC1b \sin 2\Delta u \cos \beta + T3C4uC1b \cos 4\Delta u \cos \beta \\ &\quad + T3S4uC1b \sin 4\Delta u \cos \beta \\ T2(\Delta u, \beta) &= T20S3b \sin 3\beta + T2C2uS2b \cos 2\Delta u \sin 2\beta \\ &\quad + T2S2uS2b \sin 2\Delta u \sin 2\beta \\ T1(\Delta u, \beta) &= T1S2uC1b \sin 2\Delta u \cos \beta \end{aligned}$$

- β -dependency can be ignored for short-arcs => ECOM-T
- stochastic orbit parameters (i.e., pulses or accelerations) can be added optionally => ECOM-TBP

Validation of QZS-1

- Simulated and estimated SRP coefficients have comparable characteristics (apart from singularities) and show little variations from day to day:

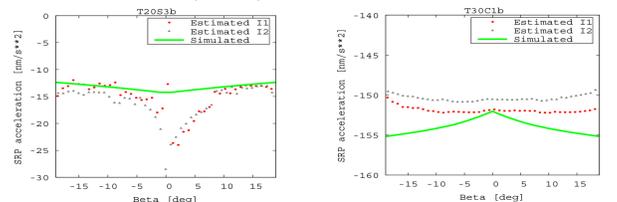


Fig. 5: Simulated vs. estimated coefficients of ECOM-TB referring to different ON-periods I1 and I2 in 2015.

- clear improvement of QZS-1 orbits and clocks:

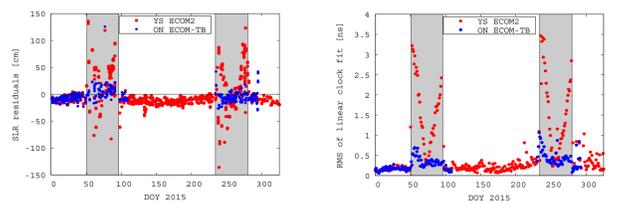


Fig. 6: Orbit and CLK-valid. of 2015 ECOM2 or ECOM-TB.

- agreement with external QZF orbit solution improves:

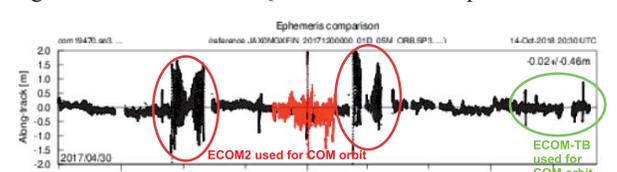


Fig. 7: QZS-1 orbit comparison betw. COM and QZF ACs (screenshot taken from <http://mgex.igs.org/analysis>)

Validation of BDS2

- smallest deviation of SRP coefficients from assumed values observed for MEOs, shorter orbit arcs, and ECOM-TBM(P)
- for IGSOs the periodic SRP coefficients are not well enough determined to represent the orbit over longer periods, which affects the remaining parameters:

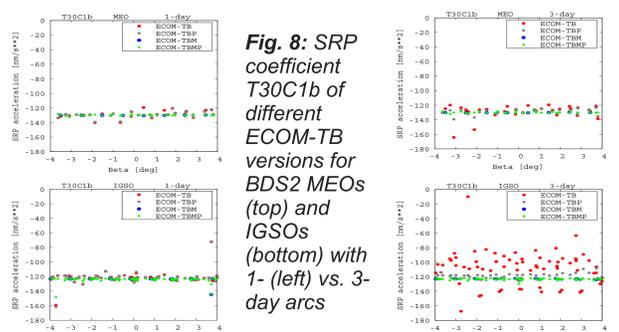


Fig. 8: SRP coefficient T30C1b of different ECOM-TB versions for BDS2 MEOs (top) and IGSOs (bottom) with 1- (left) vs. 3-day arcs

- consequently, the orbits are degraded as well in case the full ECOM-TB is used for long-arc POD of BDS2 IGSOs:

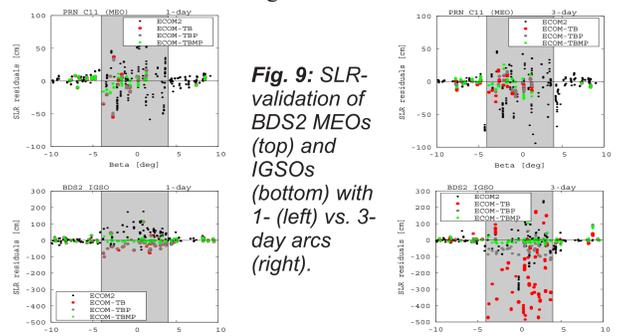


Fig. 9: SLR-validation of BDS2 MEOs (top) and IGSOs (bottom) with 1- (left) vs. 3-day arcs (right).

Validation-Summary and Conclusions

- QZS-1: ECOM-TB is a suitable stand-alone SRP model
- BDS2 MEO: addition of pulses (=>ECOM-TBP) or of an a priori box model is recommended
- BDS2 IGSO: periodic SRP coefficients cannot be estimated for long-arc orbits with current network and orbit model (=> use ECOM-TBMP or ECOM-TBM + an a priori box model)

Tab. 1: Results of orbit validation with SLR residuals (SLR), RMS of linear sat. clock fit (CLK), orbit misclosures (OMC), and 3-day long-arc fit (ORB-fit) for BDS2 IGSO (BI), BDS2 MEO (BM), and QZS-1 (Q1) satellites with different SRP models during ON-periods in 2014 and 2015.

Vali.-Method	SLR, IQR [cm]	CLK-fit, median [ns]	OMC, median [cm]	ORB-fit, med. [cm]
Sat.-System	BI BM Q1	BI BM Q1	BI BM Q1	BI BM Q1
ECOM2	20.5 21.0 62.0	1.72 1.43 1.61	55.9 29.2 42.4	23.0 10.1 14.1
ECOM-TB	- - 15.2	- - 0.35	- - 14.2	- - 5.6
ECOM-TBP	- 12.2 - -	- 0.69 - -	- 9.8 - -	- 6.8 - -
ECOM-TBMP	12.2 - -	0.72 - -	27.1 - -	44.0 - -

Possible reasons for reduced performance of ECOM-TB for BDS2:

- sampling problem for periodic SRP coefficients due to poor observation coverage over East Asia (affecting IGSOs more than globally observed MEOs; see Fig. 10)
- open questions regarding BDS orbit model (meta data!)

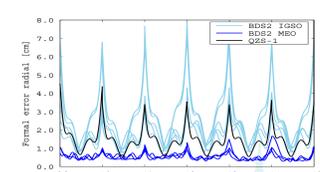


Fig. 10: Formal radial orbit error of QZS-1, BDS2 MEOs, and BDS2 IGSOs in early 2015 (YS and ECOM2 applied to all).

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Reference to COM products

Prange, L.; Arnold, D.; Dach, R.; Schaer, S.; Sidorov, D.; Stebler, P.; Villiger, A.; Jäggi, A. (2018). CODE product series for the IGS MGEX project. Published by Astronomical Institute, University of Bern. URL: http://www.aiub.unibe.ch/download/CODE_MGEX; DOI: 10.7892/thesis.75882.2.

