

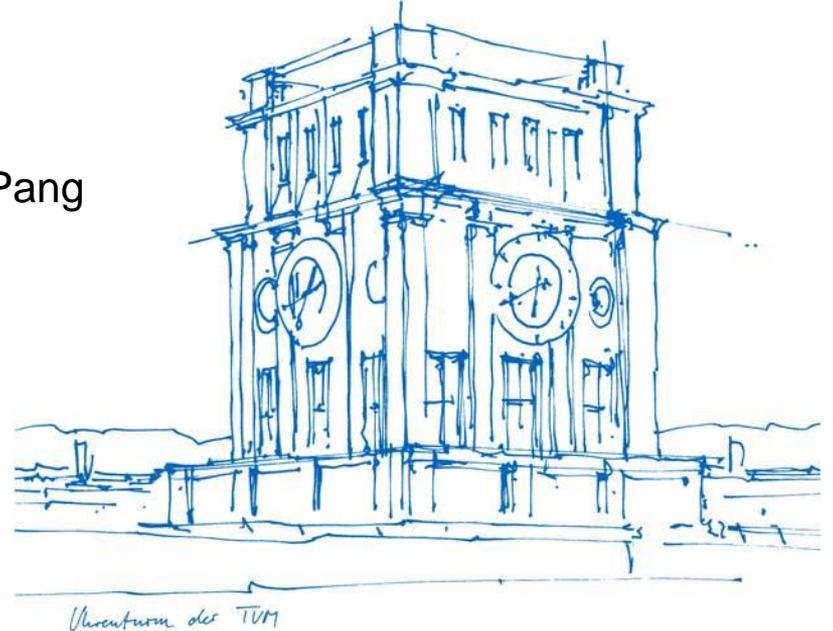
# Phase Biases of GPS L1/L2/L5 for the Purpose of Zero-difference Ambiguity Resolution and Initial Results on Galileo E1/E5a

Bingbing Duan, Urs Hugentobler, Inga Selmke, Di Pang

*Institute for Astronomical and Physical Geodesy*

*Technical University of Munich, Germany*

IGS Workshop 2018, Wuhan China, 31.Oct, 2018



Ambiguity resolution can significantly improve the quality of GNSS products and applications.

- Double-difference ambiguity resolution

Most of the errors are canceled out or may be neglected

At least two receivers are synchronously processed, miss clock info

- Zero-difference ambiguity resolution

All the error sources must be considered

Dedicated products are required



GPS L1/L2 products

- New frequencies and signals

GPS L5Q/L5X, Galileo L5Q/L5X



Preliminary results

## ➤ Phase equation of one single frequency

$$L_{r,1}^s = \rho + c(dt_r - dt^s) - I_{r,1}^s + c(\delta_{r,1} - \delta_1^s) + \lambda_1 N_{r,1}^s + \text{windup} + \text{corr}$$

Geometry distance,      Ion-delay,      Other corrections

Phase obs, Clock offsets,      Phase biases, Ambiguity

Numerous linear terms prevent direct access to the integer nature of ambiguity, double-difference can cancel out such terms fairly well

$$N_{r,1}^s = \widehat{N}_{r,1}^s + \varphi_{r,1}^s + \Delta$$

Integer value and initial shift

# Theory

## ➤ Ionosphere-free combination

Ion-free combination is used to eliminate the first order of ion-delay

$$L_{r,IF}^s = \rho + c(dt_r - dt^s) + c(\delta_{r,IF} - \delta_{IF}^s) + \lambda_{IF} N_{r,IF}^s + windup + corr$$

Double difference or  
Dedicated products(\*CNES,GFZ,WUHN)

Does not have integer character

$$N_{r,IF}^s = aN_{r,WL}^s + bN_{r,NL}^s$$

$$N_{r,WL}^s = Integer + \mu_{r,WL} - \mu_{WL}^s$$

Fix wide-lane ambiguities

$$N_{r,NL}^s = Integer + \mu_{r,NL} - \mu_{NL}^s$$

Fix narrow-lane ambiguities

\*Loyer S et al. (2012), Ge M et al. (2008), Li X et al. (2017)

# Theory

## ➤ Wide-lane biases Estimation

Melbourne-Wuebbena (MW) (Geometry-free, Ionosphere-free)

$$MW(P_{r,1}^s, P_{r,2}^s, L_{r,1}^s, L_{r,2}^s) = \lambda_{WL} \hat{N}_{r,WL}^s + \lambda_{WL} (\mu_{r,WL} - \mu_{WL}^s) + \varepsilon$$

Integer wide-lane ambiguity,      noise

Receiver bias (receiver dependent, epoch-wise)  
Satellite bias (varies slowly with time, daily)

A zero-mean constraint of all satellite biases is added

Fix single-difference ambiguities between satellites for one receiver

# Theory

## ➤ Narrow-lane biases Estimation

Introduce fixed wide-lane ambiguities into ion-free float solution  
GPS satellite orbits and clocks are fixed to CODE products

A zero-mean constraint of all the satellite biases is added

$$L_{r,IF}^s = \rho' + c(dt_r + \delta_{r,IF}) + c\delta_{IF}^s + \lambda_{nl} N_{r,nl}^s + windup + corr$$

As one clock offset

A reference ambiguity is selected every station in one session  
Fix single-difference ambiguities between satellites for one receiver

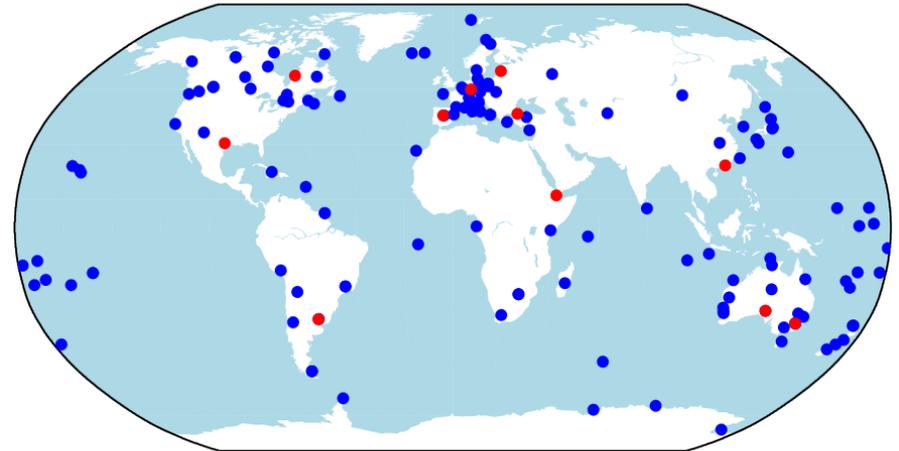
# Products of GPS L1/L2

## ➤ Settings and tracking stations

✓ **Bernese 5.3 is modified to support the estimation**

- 150 +11 tracking stations (day 200 to day 300, 2017)
- Obs type: C1C,L1C,C2W,L2W
- DCB : C1W-C1C from CODE
- Arc length: 1 day
- Orbit&clock products: CODE
- Antenna: ANTEX14
- Ambiguity fixing approach: SIGMA

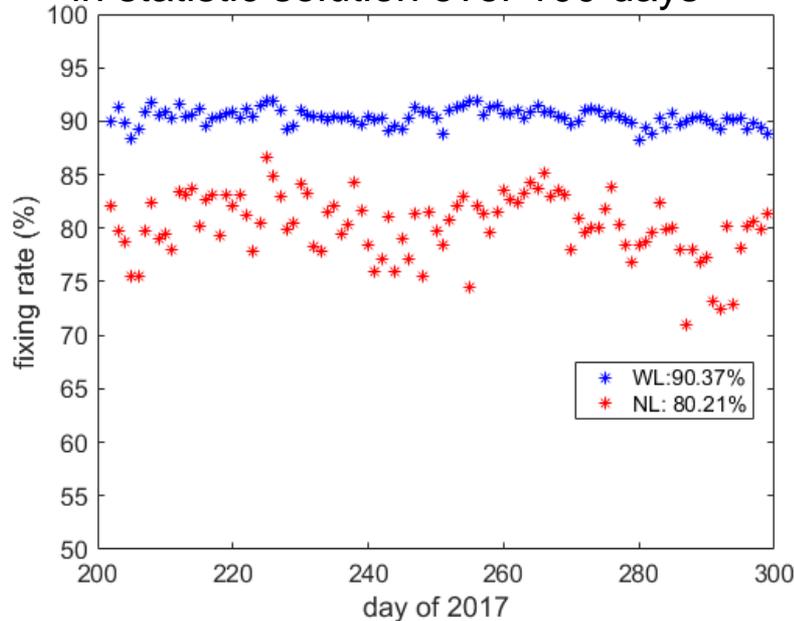
Blue for estimation, red for validation



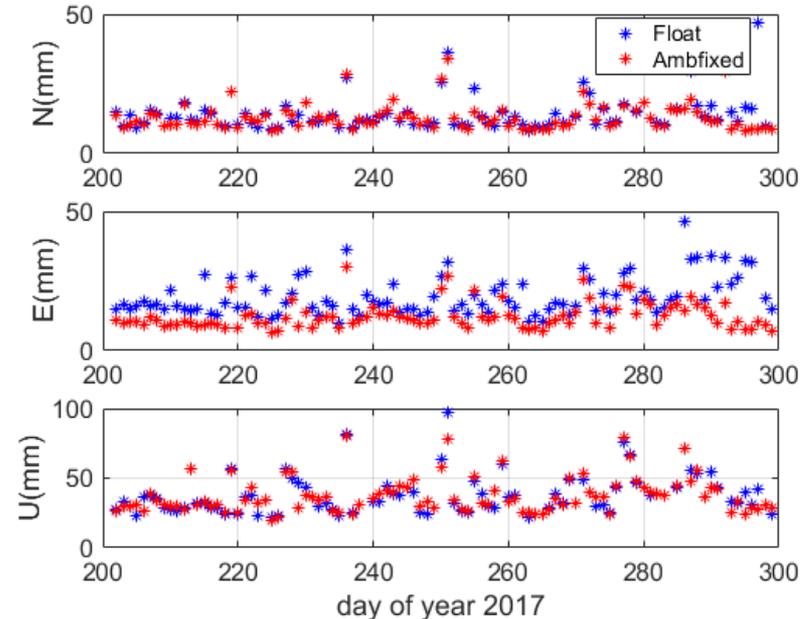
# Products of GPS L1/L2

## ➤ Application of ground tracking stations

Averaged Ambiguity fixing rate of 11 sites  
in statistic solution over 100 days



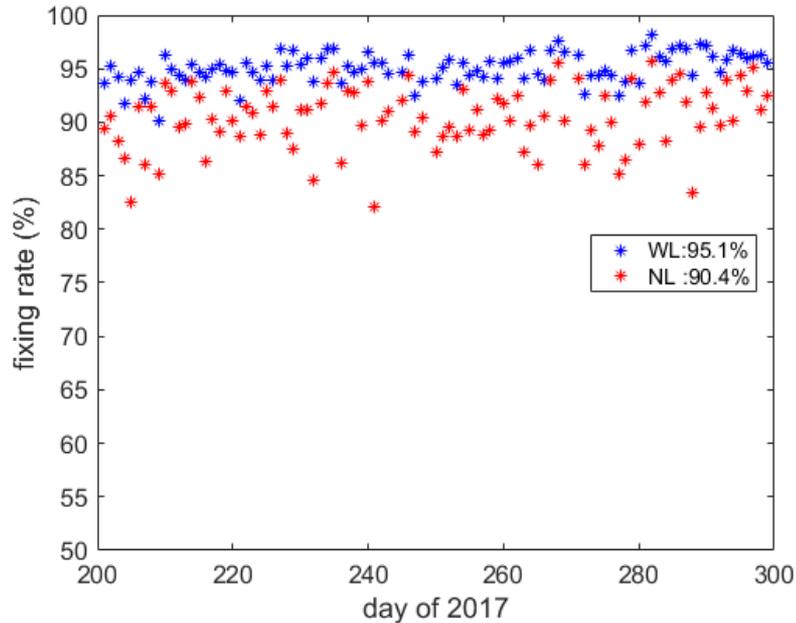
Average RMS of 11 stations over 100 days  
for kinematic solutions



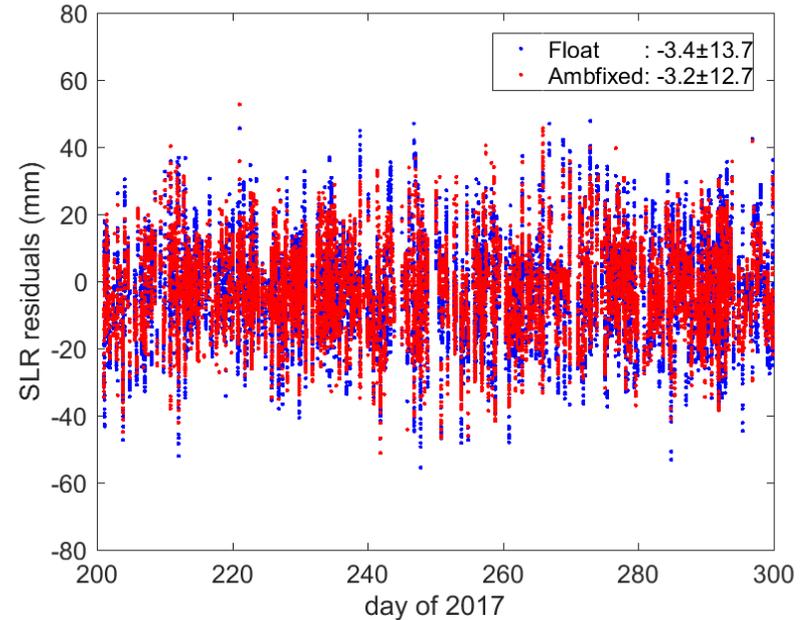
# Products of GPS L1/L2

## ➤ Application of SENTINEL-3A satellite

### Ambiguity fixing rate



### SLR residuals of reduced dynamic orbits



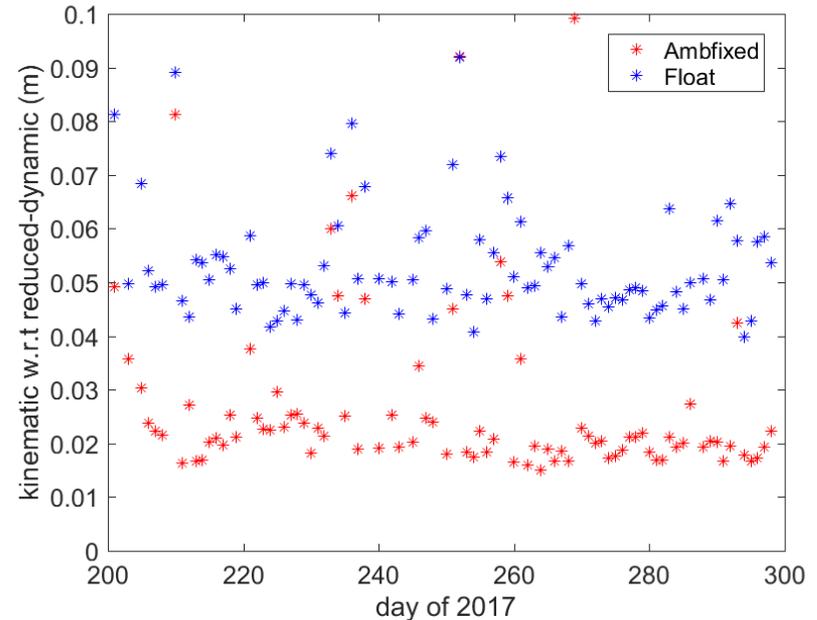
# Products of GPS L1/L2

## ➤ Application of SENTINEL-3A satellite

Ambiguity fixed reduced-dynamic solutions are taken as reference

By comparing to reduced-dynamic solutions ambiguity fixed kinematic solutions mark an improvement of more than a factor of two over the float kinematic solutions

3D difference



# Initial results of GPS L1/L5 and Galileo E1/E5a

## ➤ Issues before ambiguity resolution

1. GPS L1/L2 satellite clocks are not the same as GPS L1/L5 clocks  
(Oliver Montenbruck et al. (2011)) → Estimate L1/L5 clocks

2. LEICA, SEPT : L5Q  
TRIMBLE, JAVAD : L5X (I+Q) → Process together?

3. PCO/PCV for GPS L5 are not clear  
PCO/PCV of receivers for the GPS L1/L5 and Galileo E1/E5a

↓  
Assumed to be the same as GPS L1/L2

# Initial results of GPS L1/L5 and Galileo E1/E5a

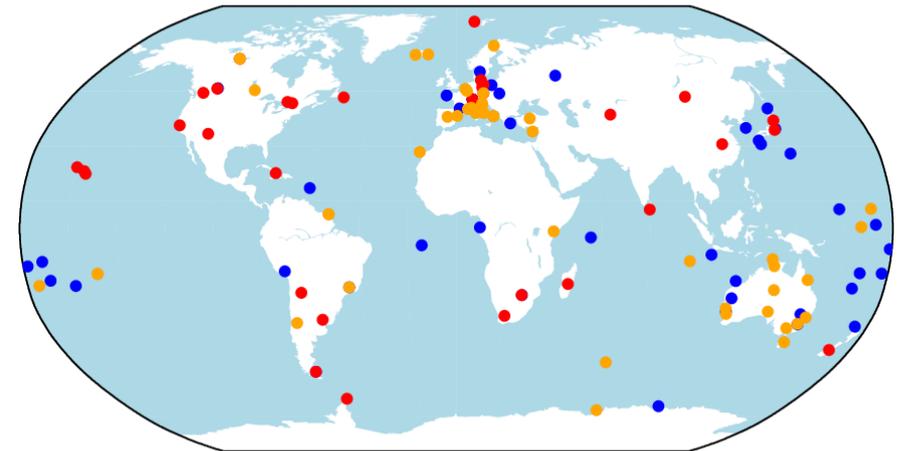
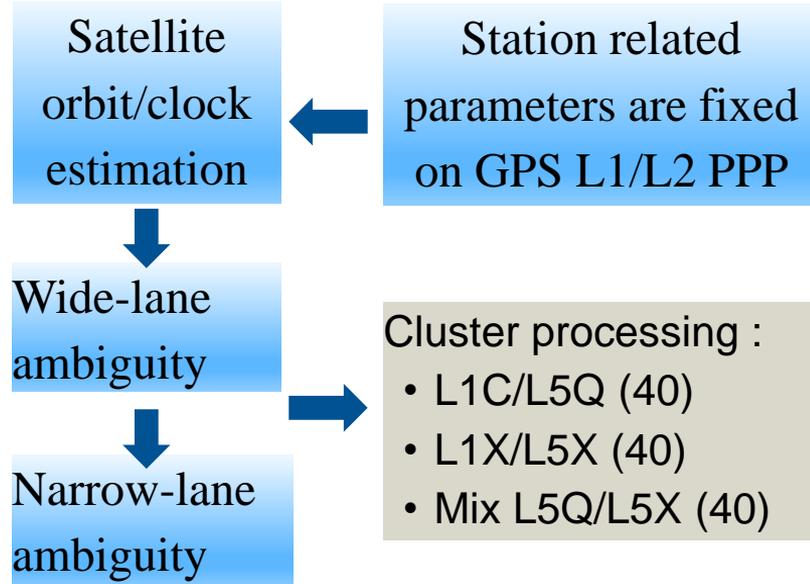
## ➤ Settings and tracking stations

Satellite : 12 GPS IIF, 17 Galileo

Blue : 42 TRIMBLE with C5X/L5X

Red : 35 JAVAD with C5X/L5X

Yellow : 45 LEICA&SEPT with C5Q/L5Q



# Initial results of GPS L1/L5 and Galileo E1/E5a

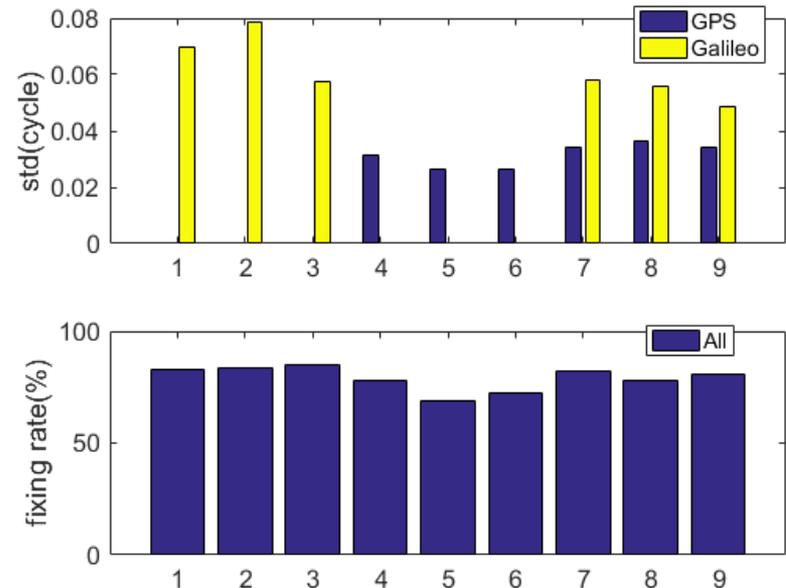
## ➤ Wide-lane biases estimation

Estimations using individual obs types

Ambiguity fixing between G and E is allowed

1. Galileo L5Q
2. Galileo L5X
3. Galileo L5Q+L5X
4. GPS L5Q
5. GPS L5X
6. GPS L5Q+L5X
7. Galileo+GPS IIF L5Q
8. Galileo+GPS IIF L5X
9. Galileo+GPS IIF L5Q+L5X

STD of wide-lane biases and average fixing rate over two weeks



# Initial results of GPS L1/L5 and Galileo E1/E5a

## ➤ Orbit validation

Galileo and Galileo+GPS L1C/L5Q

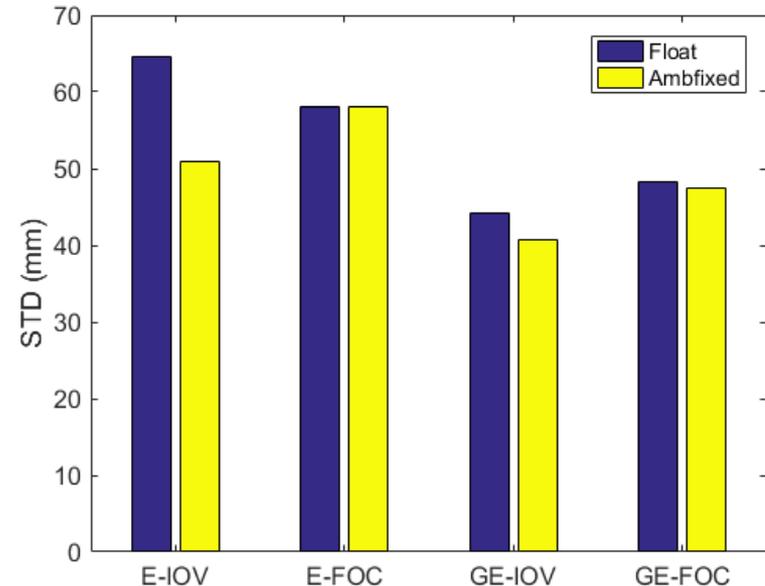
Ambiguity fixing between G and E is allowed

1. E-IOV only Galileo
2. E-FOC only Galileo
3. GE-IOV GPS IIF + Galileo
4. GE-FOC GPS IIF +Galileo

Galileo+GPS IIF results are in general better than only Galileo

Ambiguity resolution reduces the STD of SLR residuals, especially for Galileo IOV satellites

STD of SLR residuals of Galileo orbits over two weeks



# Initial results of GPS L1/L5 and Galileo E1/E5a

## ➤ Orbit validation

Galileo+GPS L1X/L5X

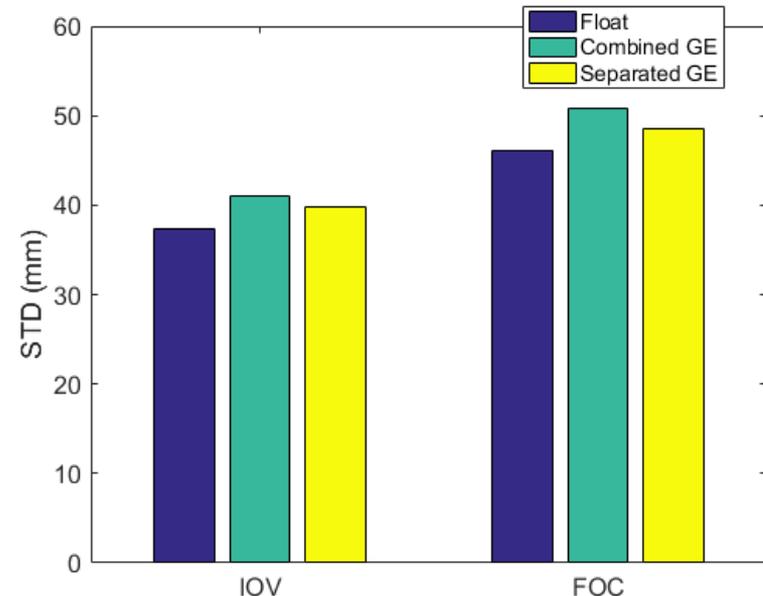
Ambiguity fixing between G and E ? Y/N

1. Combined GE **Y**
2. Separated GE **N**

Ambiguity fixing does not improve Galileo orbits by using L1X/L5X observation types

Ambiguity resolution between G and E makes results even slightly worse than the separate case

STD of SLR residuals of Galileo orbits over two weeks



# Summery and plans

1. GPS L1/L2 phase biases in TUM proves to work fairly well in zero difference ambiguity resolution.
2. Joint processing of GPS IIF and Galileo satellites with respect to the frequency L1/L5, E1/E5a improves the accuracy of Galileo orbits.
3. Ambiguity resolution between GPS and Galileo with respect to the signal L5Q and L5X needs more analysis.
4. It will be good if we can provide Galileo and GPS L1/L5 satellite orbit and clock products, or even the wide-lane biases for the purpose of zero-difference ambiguity resolution